

- (f) A star has a parallax of 0.01 *arcseconds*. Then the distance of the star will be
- (i) 3.26 light years (ii) 326 light years
(iii) 100 light years (iv) 10 light years.
- (g) The distance of the Sun from the centre of our galaxy is 8.5 *kpc*. What will be the circular velocity of the Sun around the galactic centre?
[Take the constants $A = 14.4 \text{ km s}^{-1} \text{ kpc}^{-1}$ and $B = -12 \text{ km s}^{-1} \text{ kpc}^{-1}$]
- (i) 250 km s^{-1} (ii) 224.4 km s^{-1}
(iii) 242.2 km s^{-1} (iv) 220.1 km s^{-1} .
- (h) Suppose we look at two distant galaxies : Galaxy 1 is twice as far away as Galaxy 2. In that case
- (i) We are seeing Galaxy 1 as it looked at an earlier time in the history of the universe than Galaxy 2
(ii) We are seeing Galaxy 1 as it looked at a later time in the history of the universe than Galaxy 2
(iii) Galaxy 1 must be twice as big as Galaxy 2
(iv) Galaxy 2 must be twice as old as Galaxy 1.
- (i) The dimensions of the Reynold's number is
- (i) $[M^2L^3T]$ (ii) $[ML^3T]$
(iii) $[M^2L^2T^2]$ (iv) None of these.
- (j) The expansion of the universe will be halted if the mass density of the Universe be equal to the critical density ρ_c whose value is [Take $H = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$]
- (i) $0.5 \times 10^{-29} \text{ gm cm}^{-3}$ (ii) $1 \times 10^{-29} \text{ gm cm}^{-3}$
(iii) $1.5 \times 10^{-29} \text{ gm cm}^{-3}$ (iv) $2 \times 10^{-29} \text{ gm cm}^{-3}$.

Group - B

2. Answer *any one* question : 5×1
- (a) In connection with the spherical triangle, given the observer's latitude ' φ ', the declination ' δ ' and hour angle ' H ' of the heavenly body, calculate its zenith distance and azimuth. Also given the observer's latitude ' φ ', the star's zenith distance ' z ' and azimuth ' A ', calculate the star's declination and hour angle. 3+2
- (b) Derive the fundamental formula of spherical trigonometry. 5

Group - C

3. Answer *any one* question : 5×1
- (a) Discuss the different layers of Earth's atmosphere, indicating the major constituents and their interaction with electromagnetic radiation of different wavelengths. 5
- (b) What is f/a ratio of a telescope and what are its various advantages? Compare the brightness of images of the Moon produced by two telescopes – one with $f = 200$ cm, $a = 40$ cm, and the other with $f = 600$ cm and $a = 100$ cm. 2+3

Group - D

4. Answer *any two* questions : 5×2
- (a) Define luminosity of a star. What is its relation with the effective temperature of a star? Derive the relationship between the luminosity and the absolute magnitude of a star. 1+1+3
- (b) What is stellar parallax? The apparent magnitude of a star is observed to be +3.3 and its parallax is $0''.025$. Find the absolute magnitude of the star. Compare the luminosity of this star with that of the Sun ($M_{v\odot} = +5.0$). 1+2+2
- (c) The coronal spectrum shows emission lines of intense ionization— Explain. Comment on the sources of the coronal heating. 3+2
- (d) Discuss the solar neutrino puzzle and its possible solutions. 5

Group - E

5. Answer *any one* question : 5×1
- (a) What are interstellar shock waves? Write down the equations which are appropriate for studying the propagation of a plane, normal and adiabatic shock. Deduce the Rankine-Hugoniot relation. 1+2+2
- (b) Define Jeans wavelength, λ_j and Jeans Mass M_j . How are they related to the gravitational collapse of a static homogeneous cloud? Derive expressions for them. 1+1+3

Group - F

6. Answer *any two* questions : 5×2
- (a) Derive the formulae for the radial velocity, v_r , and the tangential velocity, v_T in terms of the Oort's constants A and B . 5
- (b) Draw a diagram of the rotation curve of our galaxy and obtain a polynomial in the radial distance ' r ' that fits the rotation curve fairly well. 2+3
- (c) Describe Hubble's morphological classification of galaxies. What are the principal observable features that form the basis for this classification? What features distinguish the sub-classes? 2+2+1
- (d) Discuss the observations that suggest that a very large fraction of matter remains hidden in individual galaxies, galaxy clusters and in the universe. Also derive an estimate of the hidden matter. 3+2

Please Turn Over

Group - G

7. Answer *any two* questions :

5×2

(a) If ' m_0 ' and ' m_f ' are respectively the initial and final mass of a rocket, then prove that

$$m_f = m_0 \exp\left(-\frac{\Delta v}{c}\right),$$
 where Δv is the difference between the initial and final velocity of the rocket

and ' c ' is the velocity of exhaust.

5

(b) As an approximate of Navier–Stokes equation of motion, derive the boundary layer equations for two-dimensional incompressible fluid flow past a flat plate.

5

(c) What is Blasius boundary layer flow? Deduce the self-similar equation for this flow.

1+4

(d) Write a note on the remarkable achievements of the Indian Space Research Organization (ISRO).

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[Throughout the Paper take the Newton's Gravitational constant as $G = 6.67 \times 10^{-11} \text{ m}^3\text{kg}^{-1}\text{s}^{-2}$].
